Fuzzy control and wavelet transform-based energy management strategy design of a hybrid tracked bulldozer

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Abstract. A new hybrid system of a tracked bulldozer is designed, which primarily consists of an engine-generator set, a battery pack, and a supercapacitor. According to the power requirements of typical working conditions and the output feature of three power sources, a fuzzy control and wavelet transform-based energy management strategy is proposed. Models of the hybrid system are built in Matlab/Simulink and are then transformed into C codes, which are sent to dSPACE. The energy management strategy is verified through HILS (hardware in loop simulation), which demonstrates that the designed strategy is good for increasing the fuel efficiency of the engine and prolonging the working life of the battery pack, which can be used in the real-time control of the hybrid tracked bulldozer.

Keywords: Fuzzy control, wavelet transform, energy management, hybrid bulldozer, HILS

1. Introduction

Along with the deepening of the global energy crisis [7], exhaustion of oil resources, and aggravation of global warming problems [4], electric driving has been widely used in numerous areas, such as the automobile industry, engineering machinery, ships, and harbor hoisting machinery. Thus, the relevant energy management strategy as the core content of vehicle control has also been extensively investigated, including: (1) Rule-based Logic threshold control strategy. Based on the static torque characteristics of engines, threshold parameters are obtained, and logic control rules are built [3]. (2) Fuzzy logic control strategy. Accurate variables are transformed into fuzzy variables, and the fuzzy rules are built in this strategy. Control system outputs are

The strategies mentioned above only took the fuel efficiency, emissions, and SOC (state of charge) of the battery and the capacitor into consideration, and they neglected the frequent changes in current and required power, which impose a huge shock on batteries and the engine-generator set.

achieved through a series of algorithms, such as fuzzification, fuzzy reasoning, and defuzzification [13]. (3) Local instantaneous optimization strategy. The power consumption of a battery is converted to the fuel consumption of the battery charged by the engine, and the minimum of the equivalent fuel consumption per hour is taken as the objective function to control the output torque of the hybrid system [5]. (4) Global static optimization strategy, such as the Bellman dynamic programming and minimum (or called maximum) principle [6, 15]. The strategy relies on a given driving cycle and has a large amount of calculation, which can not be used in real automobile control and is usually used for providing reference and evaluating other control strategies.

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Aimed at a hybrid system that has three energy sources (an engine-generator set, a battery pack, and a supercapacitor), the energy management strategy is designed using fuzzy control and wavelet transform theory.

2. Structure of the hybrid tracked bulldozer

The series electric drive system with two motors driving sprockets on both sides of the tracked dozer was adopted, as shown in Fig. 1.

The system primarily consists of a general controller, an engine-generator set, a rectifier, a battery pack, a supercapacitor, two bidirectional DC/DC converters, and two driving motors and their controllers. The engine-generator set, battery pack, and supercapacitor make up the front power chain, which provides energy for the whole system. The driving motors, motors' controllers, and sprockets compose the back power chain. There is not a mechanical joint between the front and back power chain, so the electric drive structure is simple and can be easily arranged in the limited space of a bulldozer.

3. Energy management strategy design

A tracked dozer usually works in complicated conditions, and its loads change rapidly at a large scale. Using a typical operating condition as an example, the target speed, the working resistance, and the power requirement are shown in Fig. 2.

Among the three power sources of the front power chain, the engine-generator set's response is slow, and the battery pack is not suitable to charge and discharge

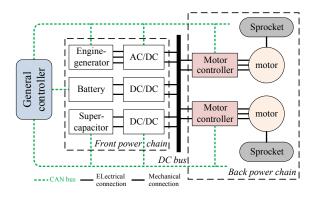


Fig. 1. Structure of the hybrid tracked bulldozer.

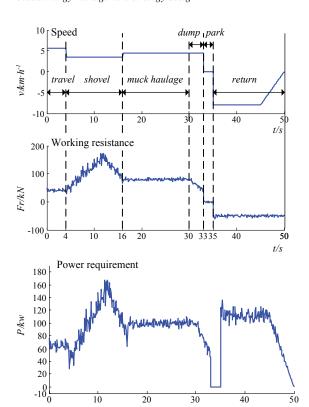
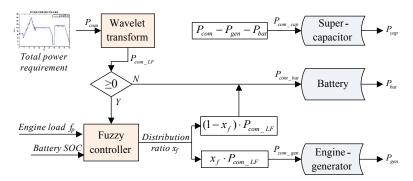


Fig. 2. A typical operating condition of a tracked dozer.

in a high frequency or with too heavy of a current [1]; therefore, neither can conveniently handle the instantaneous energy requirement. In contrast, the power density and charge-discharge cycles of the supercapacitor are much higher than those of the battery, which is good for responding quickly to instantaneous energy requirements [9, 10].

Based on the energy requirements of the back power chain and the characteristics of each power source, the energy control strategy is designed by combining fuzzy control with wavelet transform theory, as shown in Fig. 3. The low frequency part of the target power requirement (P_{com_LF}) was obtained by wavelet transform. If $P_{com_LF} < 0$, the bulldozer was in the braking state, and the feedback energy would be used to charge the battery packs. If $P_{com_LF} > 0$, it was delivered to the fuzzy controller where the outputs of the enginegenerator set and the battery packs were determined. The total power requirement minus the outputs of the engine-generator set and the battery pack would be the target output of the supercapacitor.



 $P_{com_gen}\text{-} \ \, \text{Engine-generator target output;} \\ P_{com}\text{-} \ \, \text{Total power requirement;} \ \, P_{bal}\text{-} \ \, \text{Battery output;} \\ P_{cap}\text{-} \ \, \text{Supercapacitor output;} \ \, P_{gen}\text{-} \ \, \text{Engine-generator output;} \\ P_{com_cap}\text{-} \ \, \text{Supercapacitor target output;} \ \, P_{com_bal}\text{-} \ \, \text{Battery target output.} \\$

Fig. 3. Fuzzy control and wavelet transform-based energy management strategy.

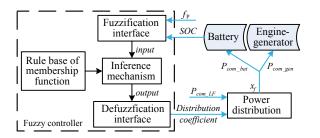


Fig. 4. Block diagram of fuzzy control strategy.

3.1. Fuzzy control

A double-inputs and single-output fuzzy control strategy is proposed in the thesis, as is shown in Fig. 4 [2]. The inputs of the fuzzy controller are the engine load f_p and the battery SOC, and the output is the power distribution coefficient x_f :

$$f_p = \frac{P_{com_LF}}{P_{gen_max}} \tag{1}$$

where P_{com_LF} is the positive low frequency part of the target power requirement, and P_{gen_max} is the maximum output power of the engine-generator set.

The target outputs of the engine-generator set and the battery packs are:

$$P_{com_gen} = x_f \cdot P_{com_LF} \tag{2}$$

$$P_{com_bat} = (1 - x_f) \cdot P_{com_LF}. \tag{3}$$

The guidelines for making the fuzzy rules are:

Reduce x_f when f_p is high and let the battery output power for supplement in time.

Raise x_f when f_p is low so as to ensure the engine works in an efficient load zone.

Maintain SOC at a value of 0.7 by regulating r_f in order to achieve a high charge/discharge efficiency. The

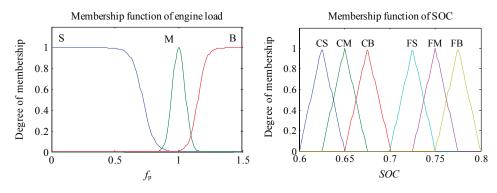


Fig. 5. The membership function of fuzzy controller inputs.

Table 1 The membership function of x_f

x_f	VS	S	RS	MS	RB	В	VB
values	0.8	0.85	0.9	0.95	1.05	1.1	1.2

Table 2
Rules based on Mamdani fuzzy control algorithm

$SOCf_p$	CS	СМ	СВ	FS	FM	FB
S	VB	VB	В	RB	М	RS
M	VB	VB	B	M	RS	S
B	VB	B	RB	RS	S	VS

membership functions of the engine load f_p and the battery SOC after fuzzification are shown in Fig. 5, which are defined as follows:

 f_p : {S, M, B}, range $[0 \sim 1]$ that presents the engine load and varies from 0 to $P_{gen-max}$.

SOC : {CS, CM, CB, FS, FM, FB}, range $[0.6 \sim 0.8]$ presents the battery SOC and varies from 0.6 to 0.8.

The definition of the distribution coefficient x_f is shown in Table 1, and eighteen rules based on the Mamdani fuzzy control algorithm were designed, as shown in Table 2.

The membership functions of fuzzy controllers greatly affect the efficiency and fuel consumption of electric drive systems. If the power management is regarded as a high dimension nonlinear optimization problem, the membership functions, which are determined by experts' knowledge, can be seen as the optimization variables [11, 14]. Therefore, in order to further improve the fuel economy, a differential evolution-based hybrid particle swarm optimization algorithm (DEHPSO) is adopted to optimize the fuzzy controller.

PSO (particle swarm optimization) is an effective evolutionary algorithm that comes in two forms: global PSO and local PSO. The velocity and position updating formulas of the global PSO can be expressed as follows [8, 12]:

$$Vg_{iD}^{k+1} = \omega_s Vg_{iD}^k + c_1 r_1 (P_{iD}^k - X_{iD}^k) + c_2 r_2 (G_D^k - X_{iD}^k)$$
(4)

$$X_{iD}^{k+1} = X_{iD}^k + Vg_{iD}^{k+1} (5)$$

where *i* is the swarm number with $i = 0, 1, ..., n_s$; *D* is the dimension number with D = 1, 2, ...d; and *k* is the iteration number. Furthermore, $Vg_i^k = [Vg_{i1}, ..., Vg_{id}]^T, X_i^k = [X_{i1}, ..., X_{id}]^T$,

 $P_i^k = [P_{i1}, \ldots, P_{id}]^T$, and $G^k = [G_1, G_2, \ldots, G_d]^T$ are the vectors of swarm velocity, swarm position, individual extreme position, and global extreme position, respectively. Furthermore, ω_s is the inertia factor that represents the degree to keep the original velocity, and $c_{1,2}$ and $r_{1,2}$ are the learning and convergence factors which are valued at 2 and 0.729 in this article, respectively. Replacing the global extreme position G_D^k with the local extreme position L_{iD}^k in Equation (4), the updated expressions of local PSO can be expressed as follows:

$$V_{iD}^{k+1} = \omega_s V_{iD}^k + c_1 r_1 (P_{iD}^k - X_{iD}^k) + c_2 r_2 (L_{iD}^k - X_{iD}^k)$$
(6)

$$X_{iD}^{k+1} = X_{iD}^k + Vl_{iD}^{k+1} (7)$$

Research shows that global PSO has advantages in calculation speed but disadvantages in premature convergence; in contrast, local PSO converges slowly, but the calculation time is too long. Based on this, a hybrid PSO that combines the two algorithms is proposed to improve optimization efficiency. The updated expressions of the hybrid PSO are shown as follows:

$$Vh_{iD}^{k+1} = bVg_{iD}^{k+1} + (1-b)Vl_{iD}^{k+1}$$
 (8)

$$X_{iD}^{k+1} = X_{iD}^k + Vh_{iD}^{k+1} (9)$$

where *b* is the combination factor. To alleviate the problem of premature convergence in the early period and slow convergence in the later period, the *b* value should be gradually increased with the iteration.

To increase the population diversity and guarantee global convergence, the particles should have an ability to mutate and crossover in a certain probability. Based on this, this paper introduces the method of differential evolution (DE) to obtain new particles by crossover and recombination between original particles. The process is described in the following:

The method of judging local convergence: The variance of particles' fitness is selected as the reference for judgment. The variance of fitness in k iteration can be defined as:

$$(\sigma^2)^{(k)} = \frac{1}{n_s} \left(\frac{f_i^k - f_{ave}^k}{q} \right)^2 \tag{10}$$

where f_i^k is the fitness of particle i, f_{ave}^k is the average fitness of particles, and q is the normalized factor. When

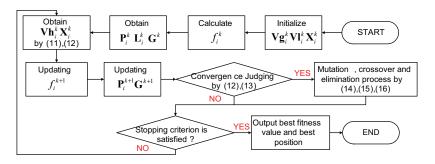


Fig. 6. Flow chart of DEHPSO.

 σ^2 is less than threshold variance σ_s^2 , the algorithm is judged for convergence.

The mutation method: Particles are mutated based on the DE theory, and the position of the new particle in the *D* dimension can be expressed as follows:

$$H_{iD}^{k+1} = X_{iD}^k + \varsigma (G_D^k - X_{iD}^k) + \upsilon (X_{i_1D}^k - X_{i_2D}^k)$$
(11)

where $i \neq i_1 \neq i_2$, and ζ and υ are zoom factors that affect the convergence rate and diversity of population, respectively.

The crossover method: The mutated particle and its original particle are chosen as the crossover objects, and the cross operation is completed by exchanging position coordinates in random dimensions. The particle position in *D* dimension after crossover is:

$$C_{iD}^{k+1} = \begin{cases} H_{iD}^{k+1} & random \ge CROSS \text{ or} \\ D = D_{rand} \\ X_{iD}^{k} & \text{otherwise} \end{cases}$$
 (12)

where CROSS is the cross probability, random is a random number generated by the system, and D_{rand} is a preset cross location.

The elimination method: After the mutation and crossover operations, the newly created particles are compared to the original particles in order to eliminate those that have a worse fitness; this process can be described as follows:

$$X_{iD}^{k+1} = \begin{cases} C_{iD}^{k+1} & \text{if } f_{\mathbf{C}_i^{k+1}} & \text{is better than } f_{\mathbf{X}_i^k} \\ X_{iD}^k & \text{otherwise} \end{cases} . \tag{13}$$

The specific flow of DEHPSO is described in Fig. 6.

The optimization target in this paper is to minimize the fuel consumption after a certain working time, and SOC is also an important factor that influences the fuel

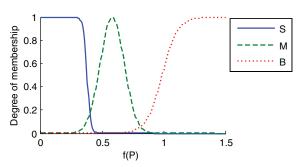
consumption (when the fuel consumption is forcibly reduced, the battery undertakes more tasks, and the SOC of which will decrease); therefore, variance of SOC (Δ SOC) should be limited in a short interval to ensure the optimization effect. The optimization function (or fitness value) can be expressed as follows:

$$f_i = m_i V_e \quad \Delta SOC \in [-\varepsilon, +\varepsilon].$$
 (14)

The optimized membership functions are shown in Table 3 and Fig. 7.

Table 3 The optimized membership function of x_f

$\overline{x_f}$	VS	S	RS	M	RB	В	VB
values	0.8	0.8291	0.8736	0.8804	0.9398	1.0912	1.2



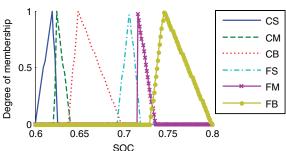


Fig. 7. The optimized membership function of fuzzy controller inputs.

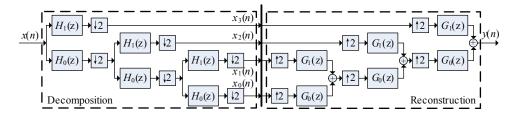


Fig. 8. The decomposition and reconstruction processes of the 3-order Haar DWT.

3.2. Wavelet transform

As the power requirement signal is discrete in one dimension, the discrete wavelet transform (DWT) is used to decompose it in different levels. The DWT and IDWT (inverse discrete wavelet transform) are:

$$W(\lambda, u) = \int x(t) \frac{1}{\sqrt{\lambda}} \Phi(\frac{t - u}{\lambda}) dt$$
 (15)

$$x(t) = \sum_{j \in \mathbb{Z}} \sum_{k \in \mathbb{Z}} W(j, k) \Phi_{j,k}(t)$$
 (16)

where x(t) is the original signal; λ is the scale factor, $\lambda = 2^j$, $j \in Z$; Φ is the mother wavelet; μ is the shift factor, $\mu = k2^j$ and j, $k \in Z$; and finally, W is the wavelet coefficient.

Compared to other common wavelets, the generating function of the Haar wavelet has the shortest filter length in the time domain, and the transformation and the inverse transformation are the same. Thus, the decomposition process of the Haar wavelet is much simpler than those of other wavelets, which makes it feasible to

extract transient signals in real-time control of the electric drive bulldozer. The expression of the Haar wavelet is:

$$\Phi(t) = \begin{cases} 1 & t \in (0, 0.5) \\ -1 & t \in (0.5, 1) \\ 0 & \text{others} \end{cases}$$
 (17)

A two-channel filter bank based on the Haar wavelet was adopted. The original signal x(t) is decomposed into reference signals and detail signals by a low-pass filter $H_0(z)$ and a high-pass filter $H_1(z)$, and the signal is rebuilt by a reconstruction filter bank $[G_1(z), G_0(z)]^T$. The decomposition and reconstruction processes of the 3-order DWT based on the Haar wavelet are shown in Fig. 8. Only eight sampling points of power requirement (which is composed of one point in current time and the previous seven points) are necessary for the 3-order DWT. There is no need to know the whole working condition in advance, which is superior to Fourier transform. The DWT could also be used for processing signals in unknown working conditions.

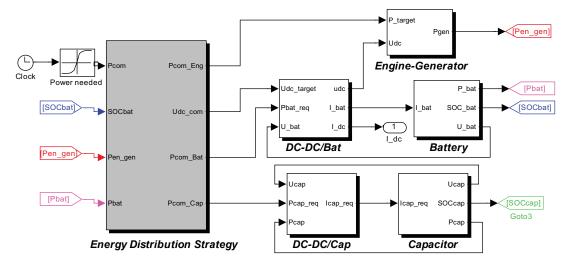


Fig. 9. Models built in Matlab/Simulink.

4. Modeling and simulation

4.1. HILS platform

The simulation platform of the hybrid system was built in MATLAB/Simulink, which primarily consists of a control strategy model, an engine-generator set model, a battery pack model and its DC/DC model, and a supercapacitor model and its DC/DC model, as shown in Fig. 9.

4.1.1. Engine-generator set model

The engine and generator are modeled as a whole according to the rotation speed relationship between them. The generator is connected to the DC bus through a three-phase bridge uncontrolled rectifier with a filter capacitor, and the equivalent circuit of PMSM (permanent magnet synchronous motor) with a bridge rectifier is shown in Fig. 10.

The internal resistance and torque losses of the generator are neglected, and the voltage of the DC bus and the electromagnetic torque are:

$$\begin{cases}
U_{DC} = K_e \omega_g - K_x \omega_g I_{DC} \\
T_e = K_e I_{DC} - K_x I_{DC}^2
\end{cases}$$
(18)

where $K_e\omega_g$ is the induced electromotive force, $K_x\omega_g$ is the equivalent resistance, and I_DC is the current of the DC bus.

4.1.2. Battery pack model

As the electric energy storage unit of the electric drive system, the main functions of the battery pack are supplying power when the engine is unable to respond to the power requirement and recycling the braking energy of the driving motors. The battery pack provides or accepts energy according to the control signals from the general controller, and it sends signals of SOC in current time and the maximum charge-discharge power limit

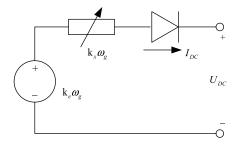


Fig. 10. Equivalent circuit of the engine-generator set.

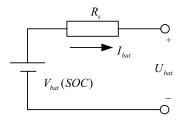
to the general controller. The battery pack is connected to the DC bus through a DC/DC converter. The equivalent resistance model is adopted, as is shown in Fig. 11. The battery pack is equivalent to an ideal voltage source with a series resistance:

$$U_{bat} = V_{bat} - I_{bat} R_s. (19)$$

Both the open-circuit voltage V_{bat} and the equivalent resistance R_s vary by changes in the SOC and the temperature; however, the effect of temperature is small and can be neglected when modeling. V_{bat} and R_s are obtained through lookup tables by inputting the SOC, and the SOC of the battery pack is calculated by the ampere-hour integration approach:

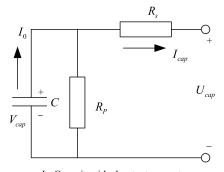
$$SOC(t) = \frac{Q_0 - \int_0^t i(\tau)d\tau}{Q_{\text{max}}}$$
 (20)

where SOC(t) is the battery's SOC of current time, Q_0 is the initial capacity of the battery, $i(\tau)$ is the battery's charge-discharge current, and Q_{max} is the maximum capacity of the battery.



 V_{bat} - Open-circuit voltage; R_s - Equivalent internal resistance; I_{bat} - Battery output current; U_{bat} - Battery terminal voltage.

Fig. 11. Equivalent circuit model of the battery pack.



 I_{0} - Capacitor ideal output current; I_{cap} - Capacitor actual output current; C- Equivalent capacitance; V_{cap} - Open-circuit voltage; R_{s} - Equivalent series resistance; R_{I} - Equivalent parallel resistance.

Fig. 12. Equivalent RC model of the supercapacitor.

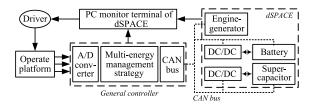


Fig. 13. Structure of the driver-controller-based HILS.

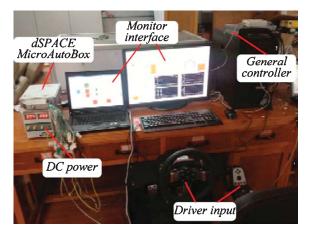


Fig. 14. Hardware of HILS platform.

4.1.3. Supercapacitor model

The equivalent RC model is adopted and is shown in Fig. 12. Based on the equivalent circuit, the output current is:

$$I_{cap} = I_0 - \frac{1}{R_P C} \int I_0 dt \tag{21}$$

The series resistance of the supercapacitor changes little when charging and discharging and is usually taken as a constant. The parallel resistance is small, which has less of an effect on the circuit and is usually ignored. The SOC of the supercapacitor is:

$$SOC = \frac{V_{cap} - V_{\min}}{V_{\max} - V_{\min}} \tag{22}$$

where V_{min} and V_{max} are the minimum and maximum open-circuit voltages of the capacitor, respectively.

By choosing driver input equipment and testing the controller as hardware, the HILS platform is established based on dSPACE Micro-AutoBox 1401/1504, and the structure of which is shown in Fig. 13. Models of the engine-generator set, the battery, and the supercapacitor built in host computer are compiled and downloaded into dSPACE by the Matlab/RTW interface. The control strategy model is first compiled by Matlab/Stateflow and then transcoded by TargetLink and downloaded into the tested controller.

After processing of A/D conversion, the controller receives the signals and communicates with dSPACE by USB CAN. The hardware components of the HILS platform are shown in Fig. 14. To obtain the driving states of the dozer, a monitor interface is built in a monitor terminal based on Controldesk, which is shown in Fig. 15.

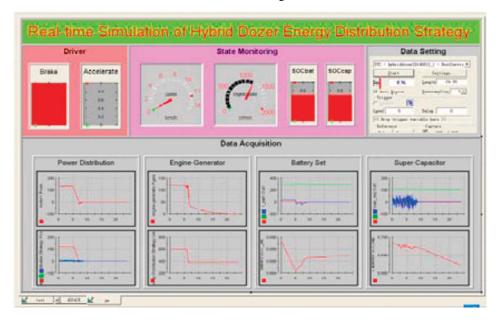


Fig. 15. ControlDesk monitoring interface.

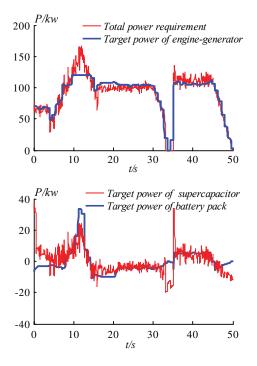


Fig. 16. Power distribution result of the front power chain.

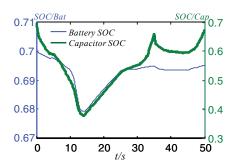


Fig. 17. SOC changes of battery and supercapacitor.

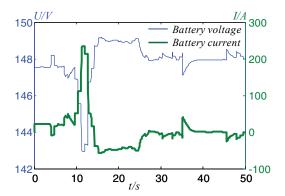


Fig. 18. Current and voltage of the battery.

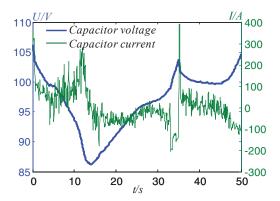


Fig. 19. Current and voltage of the capacitor.

4.2. Simulation results

The power distribution result of the front power chain is shown in Fig. 16. As the main power source, the engine-generator set is expected to provide most of the power requirement. As the auxiliary power unit, the battery pack affords power when the engine-generator's output is not sufficient and recycles energy when braking, which plays a role in peak shaving and valley filling. The supercapacitor, which has the advantage of fast charging and discharging, is required to respond to the instantaneous power requirement.

The SOC curves of the battery pack and the supercapacitor are shown in Fig. 17. It is observed that the battery SOC changes little and essentially stabilizes around 0.7, and the supercapacitor SOC changes in a wide range from 0.4 to 0.75. The supercapacitor's advantages of fast discharging and deep discharging are exhibited. The charge-discharge voltage and current of the battery and the supercapacitor are shown in Figs. 18 and 19, respectively. The charge-discharge current of the battery varies from –100 A to 250 A, which is more stable than that of the supercapacitor that varies from –200 A to 400 A.

5. Conclusions

The fuzzy control and wavelet transform-based energy management strategy of the hybrid tracked bulldozer is proposed, which realizes the energy distribution among the engine-generator set, battery pack, and supercapacitor according to the changing frequency of the required power and thus improves the system performance and prolongs the service life of the components. Modeling and HILS are conducted, and

the results show that the designed strategy can properly distribute power and is suitable for the real-time control of a hybrid dozer.

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