

Erratum

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## Symbolic protocol analysis with an Abelian group operator or Diffie–Hellman exponentiation

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The authors are grateful to Stéphanie Delaune and Ralf Treinen for noticing flaws in our constraint solution procedure. In Section 6.4, if there is a derivation constraint  $T \triangleright u$  such that  $u$  contains the first occurrence of a variable  $x$ , a new variable  $\hat{x} = u$  is introduced to eliminate  $x$ . This leads to some problems. First, the substitution may create new solutions, making the step unsound. Second, the substitution may lose solutions, making the procedure incomplete.

For example, the system

$$\begin{aligned} a^3 &\triangleright X^2 \\ a^3, X^2 &\triangleright a^3 \end{aligned}$$

does not have a solution, but after setting  $\hat{X} = X^2$  so that  $X = \hat{X}^{1/2}$ , the new system is trivially solvable. However, there is no substitution for  $X$ . The fix for this is to require a solution to  $u \triangleright \hat{x}$ , generating additional Diophantine equations.

Incompleteness is illustrated by the system

$$\begin{aligned} a^2 &\triangleright X^2 \\ a^2, X &\triangleright a \end{aligned}$$

which has the solution  $X = a$ , but after replacing  $X^2$  with  $\hat{X}$  to get

$$\begin{aligned} a^2 &\triangleright \hat{X} \\ a^2, \hat{X}^{1/2} &\triangleright a \end{aligned}$$

the Diophantine equation for the second constraint above is written (incorrectly) as though  $\hat{X}^{1/2}$  is expressible as an integer power of  $a^2$ , leading to an equation in exponents  $2z = 1$  which is not solvable in integers.

The authors are working on a revision of this section to address these problems, which we expect to have ready for the following issue.