

Predicting the minimal inhibitory concentration of fluoroquinolones for *Escherichia coli* using an accumulation model

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Abstract. The objective of this study is to evaluate whether the accumulation model developed by Zarfl et al. (2008) could be used to predict the minimal inhibitory concentration (MIC) of a group of antibacterial fluoroquinolones (FQs) for *Escherichia coli* (*E. coli*). Our model, which is based on the “Fick-Nernst-Planck” equation and the permeability of the neutral and charged species as well as the physicochemical parameters of the FQs, could predict $1/\text{MIC}_{90}$ using a linear function. It is envisaged that in the drug development projects of new FQs, the accumulation model described in this study could be utilized as an effective tool to enable early assessment of MIC value using physicochemical parameters.

Keywords: Fluoroquinolones, minimal inhibitory concentration, *Escherichia coli*, physicochemical parameters

1. Introduction

Fluoroquinolones (FQs) are broad spectrum antimicrobial agents which are active against many Gram-positive and Gram-negative bacteria [1]. These molecules contain one acid and one base with the protonation macroconstants close to each other. Figure 1 shows four different pH-dependent protonation states of the molecule, namely cation (H_2X^+), zwitterions (HX^\pm), neutral species (HX^0) and anion (X^-). The mole fractions of the zwitterionic and neutral species reach the maximal amount at the isoelectric point while their ratio is invariable and pH-independent. It has been reported that the antibacterial potency of FQ are predominantly driven by the concentration of the drug in proximity to the intercellular targets [2,3].

There is a great demand for new antibiotics to address emerging bacterial infections [3,4]. In the development of antibiotics, one of the frequently used approaches is to enhance the potency by modifying the existing antimicrobial agents, such as FQs [5]. The microbiological potency of the compounds would be assessed by using the minimum inhibitory concentration (MIC) for the pathogen. MIC is defined as the lowest concentration of an antimicrobial agent that will inhibit the visible

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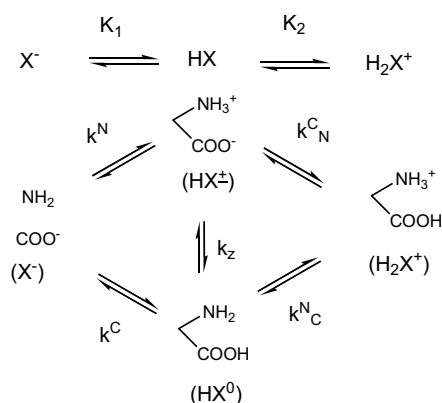


Fig. 1. Ionization scheme of a diprotic amphoteric molecule.

growth of a microorganism at an endpoint of overnight incubation [6]. In practice, it usually refers to the lowest concentration that inhibits 50% (MIC_{50}) or 90% (MIC_{90}) of bacterial colonies or isolates and can indicate shifts in the susceptibility of bacterial populations to antimicrobial agents. Therefore, the mechanistic rationalization of the factors driving the MIC values, and the ability to predict these values reliably would be of considerable interest in the course of developing antimicrobial agents.

Trapp and others [7–10] have modeled the flux of neutral and ionic compounds into cells by employing a dynamic cell model based on the “Fick-Nernst-Planck” formula. Interestingly, Zarfl et al. [11] have adopted this model to simulate the accumulation of antibacterial sulfonamides in *Escherichia coli* (*E. coli*) based on various assumptions on the permeability of the neutral and ionized species. In this work, we seek to extend the accumulation model to study the MIC values of a set of FQs for *E. coli*. In particular, the neutral, the zwitterionic and the ionized species of the FQs will be considered independently with their permeability values estimated using the physicochemical parameters of the compounds. As far as we are aware, the accumulation model has not been applied to study FQs.

2. Materials and methods

2.1. Drugs and chemicals

Moxifloxacin was supplied by AstraZeneca (Alderley Park, UK). Norfloxacin, lomefloxacin, ofloxacin, pefloxacin, sparfloxacin, gatifloxacin and other chemicals were supplied by Sigma-Aldrich (St. Louis, US).

2.2. Determination of protonation macroconstants

The protonation macroconstants were determined by means of pH-metric titrations (GLpK_a instrument, Sirius, Forest Row, UK).

2.3. Determination of protonation microconstants

The protonation microconstants were determined by means of UV-titrations. As shown in Figure 1, the microconstant, k^C , is influenced by the protonation state of the carboxylate group, which can be detected by selective spectrophotometric monitoring of the spectral region of 320–350 nm. The $\log k^C$ value was derived by using Eqs. (1) and (2):

$$\alpha_{\text{COO}^-(\text{pH})} = \frac{A_{(\text{COO}^-)} - A_{(\text{pH})}}{A_{(\text{COO}^-)} - A_{(\text{COOH})}} \quad (1)$$

$$k^C = \frac{\alpha_{\text{COO}^-(\text{pH})} (1 + K_1[\text{H}^+] + K_1K_2[\text{H}^+]^2) - K_1K_2[\text{H}^+]^2}{[\text{H}^+]} \quad (2)$$

where $A_{(\text{COO}^-)}$ and $A_{(\text{COOH})}$ represents, respectively, the experimental absorbance values at a pH in which the acid group is fully deprotonated and fully protonated. The symbol $\alpha_{\text{COO}^-(\text{pH})}$ represents the degree of protonation at the pH in which the absorbance value is denoted as $A_{(\text{pH})}$. With the $\log k^C$ value determined (see Eq. (2)), the other microconstants can be derived by using Eqs. (3) and (4):

$$K_1 = k^C + k^N \quad (3)$$

$$K_1K_2 = k^Ck^Nc = k^Nk^C_N \quad (4)$$

In addition, the ratio of the concentration of zwitterions species to that of the neutral species, which is defined as the tautomer ratio (k_z), could be calculated by Eq. (5):

$$k_z = \frac{k^N}{k^C} = \frac{k^Nc}{k^C_N} \quad (5)$$

2.4. Measurement of partition coefficients

The n-octanol/water partition coefficient at the isoelectric point ($\log D^{\text{iepH}}$) was determined by using the shake-flask technique. The $\log D^{\text{iepH}}$ value was calculated as follows:

$$\log D^{\text{iepH}} = \log \left[\frac{A_0 - A_1}{A_1} \left(\frac{V_{\text{aq}}}{V_{\text{oct}}} \right) \right] \quad (6)$$

where A_0 and A_1 denote the UV/visible absorbance value, before and after partition, at the maximal absorption of the chemical in the aqueous environment, respectively. $V_{\text{aq}}/V_{\text{oct}}$ represents the ratio of aqueous volume to n-octanol volume.

2.5. Accumulation model

The uptake rate (k_u) of the drug across the bacterial cell wall and the release rate (k_r) of the drug to the environment are taken into consideration in the accumulation model developed by Zarfl et al. [11]. At steady state in which the rate of change of drug concentration (C) within the bacterial cell is zero, the accumulation factor (AF) can be defined as follows:

$$AF = \frac{C_{cell}}{C_{env}} = \frac{k_u}{k_r} \quad (7)$$

$$k_r = P_0 \gamma_0 f(0)_{cell} + P_{\pm} \gamma_0 f(\pm)_{cell} + P_+ \frac{N_+}{e^{N_+} - 1} \gamma_+ f(+)_{cell} e^{N_+} + P_- \frac{N_-}{e^{N_-} - 1} \gamma_- f(-)_{cell} e^{N_-} \quad (8)$$

$$k_u = P_0 f(0)_{env} + P_{\pm} f(\pm)_{env} + P_+ \frac{N_+}{e^{N_+} - 1} f(+)_{env} + P_- \frac{N_-}{e^{N_-} - 1} f(-)_{env} \quad (9)$$

where the subscripts *cell* and *env* denote, respectively, the cell and environment pH. The intracellular pH is set at 7.6 for bacterial cytoplasm [12], while the environment pH is arbitrarily defined at 6. The symbol γ represents the activity coefficient of the respective species in the cell ($\gamma_0 = 1.23$; $\gamma_- = \gamma_+ = 0.74$, assuming the ionic strength of the cytoplasm of *E. coli* is about 0.3 M). N is defined as $z \times E \times F / (R \times T)$, with z the electric charge (+1 for cations, -1 for anions), F the Faraday constant (96484.56 C mol⁻¹), R the universal gas constant (8.314 J mol⁻¹ K⁻¹), T the absolute temperature (K) and E the membrane potential for *E. coli* which is about -0.11 V [12] ($N_+ = -4.28$; $N_- = 4.28$).

The symbols f and P represent, respectively, the fraction of the species with respect to the corresponding charge types and the permeability of these species across the bacterial cell wall. The fraction of the species as a function of pH can be calculated using the protonation microconstants of the corresponding FQs [13]. The permeability of the neutral species across the bacterial cell wall is estimated as follows [11]:

$$\log P_0 \approx \log D^{iepH} - 6.30 \quad (10)$$

The permeability of the zwitterionic and the ionic species are calculated as follows:

$$\log P_{\pm} = \log P_0 - \delta_{ZW} \quad \text{and} \quad \log P_{+} = \log P_{-} = \log P_0 - \delta_{ion} \quad (11)$$

where δ_{ZW} and δ_{ion} are treated as adjustable parameters in our analysis.

3. Results and discussion

3.1. Physicochemical parameters of fluoroquinolones

Table 1 depicts the physical properties of the FQs studied in this paper, including log K , log k and log D^{iepH} . It shows that the k_z ranges from 1.8 to 15.9, which indicated the preference of zwitterion in-

Table 1
Physical properties and antibacterial potency of the fluoroquinolones

Compound	log K ₁	log K ₂	pH _{IEP}	log k ^C	log k ^C _N	log k ^N	log k ^N _C	k _z	log D ^{iePH}	MIC ₉₀ (μg/mL <i>E. coli</i>)
Norfloxacin	8.52 ± 0.01 ^a	6.29 ± 0.01	7.4	7.94 ± 0.09	6.43	8.38	6.87	2.75	-1.07	0.12 ^b [14,15]
Lomefloxacin	8.93 ± 0.01	5.83 ± 0.01	7.4	8.32 ± 0.11	5.96	8.80	6.44	3.02	-1.13	0.50 [16]
Ofloxacin	8.14 ± 0.01	6.03 ± 0.01	7.1	7.18 ± 0.13	6.08	8.09	6.99	8.13	-0.44	0.12 [14]
Pefloxacin	7.51 ± 0.01	6.26 ± 0.01	6.9	6.70 ± 0.14	6.35	7.42	7.07	5.25	0.37	0.25 [14]
Sparfloxacin	8.97 ± 0.01	6.32 ± 0.01	7.6	8.52 ± 0.09	6.52	8.77	6.77	1.78	-0.09	0.13 [16]
Gatifloxacin	9.13 ± 0.01	5.97 ± 0.01	7.6	7.90 ± 0.06	6.00	9.10	7.20	15.85	-0.71	0.10 [17]
Moxifloxacin	9.32 ± 0.01	6.28 ± 0.01	7.8	8.23 ± 0.11	6.32	9.28	7.37	11.22	-0.26	0.06 [18]

^a Uncertainty was calculated as the standard deviation of the results obtained from 3 different experiments.

^b Numbers in brackets referred to the source of the MIC₉₀ data (see reference section).

aqueous phase. Thus, zwitterion of the FQ molecule is the dominating species across the physiological pH region, which is consistent with the low and moderate lipophilicity values (log D^{iePH}) as determined in this study.

3.2. Modeling the MIC values

Table 1 shows the MIC₉₀ values of the studied FQs for *E. coli*, cited from several references. For gram-negative organisms (*E. coli*), the antibacterial agent must penetrate the outer lipid membrane and overcome the evasion of efflux pumps. It is generally considered that, in gram-negative bacteria, the porin proteins act as a principal entry pathway [19]. Polar species are expected to be able to enter the bacterial cell wall through these hydrophilic channels.

Assuming the bacterial cell metabolism does not affect the accumulation for the FQs significantly,

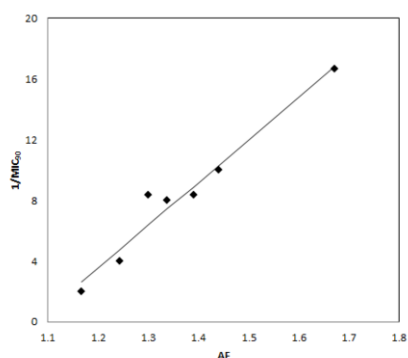


Fig. 2. Comparison of 1/MIC₉₀ of the selected fluoroquinolones with the accumulation factor (AF).

the antibiotic effects would be enhanced with the increase of drug accumulation in the cell. A regression analysis of AF (see Eq. (7)) against $1/\text{MIC}_{90}$ was carried out by treating δ_{ZW} and δ_{ion} (see Eq. (11)) as adjustable parameters. As shown in Figure 2, a plot of $1/\text{MIC}_{90}$ as a function of AF exhibits a reasonably linear relationship, suggesting the generality of the model. It was found that the regression calculation converged to a global solution with $\delta_{\text{ZW}} = 0.38$ and $\delta_{\text{ion}} = 0.57$, which are much smaller than that proposed by Zarfl et al. for the antibacterial sulfonamides [11]. Obviously, the smaller the δ value is, the closer the permeability of the ionic species to that of the neutral species would be (see Eq. (11)). This suggests that the zwitterionic, the cationic and the anionic species of FQs, play an important role in penetrating the bacterial cell wall to elicit the antibacterial effects in gram-negative organisms.

3.3. Implications of our model

Assuming the FQs process the same pharmacophore, it is very likely that the molecule binds to the target sites within the bacterial cell by means of a similar binding mode. Thus, the target affinity may be driven by lipophilicity. Early attempts by Taléns-Visconti et al. have demonstrated a bilinear relationship between $1/\text{MIC}$ and the distribution of constant D (at pH 7) on selected FQs [20]. However, little mechanistic insight can be obtained from this kind of empirical study. With the aid of the accumulation model, our treatment enables us to rationalize the contributions of the zwitterionic, the cationic and the anionic as well as the neutral species in the permeation of the bacterial cell wall.

We envisage that our model can be used to predict the MIC values in developing new FQs, well ahead of microbiological potency evaluations. These estimates could be helpful for the identification of the potent compounds for subsequent microbiological potency, pharmacokinetic and pharmacodynamics evaluations.

4. Conclusion

We have developed an accumulation model based on the physicochemical parameters of a set of FQs. The model was able to correlate the accumulation data with $1/\text{MIC}$ of FQs for *E. coli*. Our results suggest that the model could be beneficial to enable an early prediction of the MIC in the course of developing new FQs. The early MIC estimates would have great potential to help prioritizing the most prospective research chemicals and hence offer the optimal opportunity to distinguish new FQs with the anticipated MIC value. The feasibility of the accumulation models developed in this paper is well justified by the good agreement between the calculated data and literature.

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